

Handling Derivative Instruments in Performance & Attribution

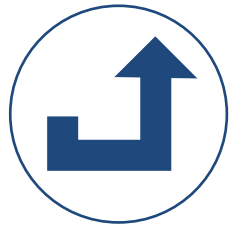
Claude Giguère



Investment Performance Solutions

Richer ● Better ● Easier

About Robust Technologies



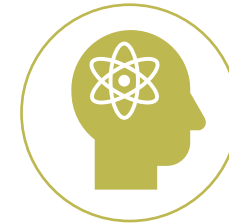
Founded
in 2006



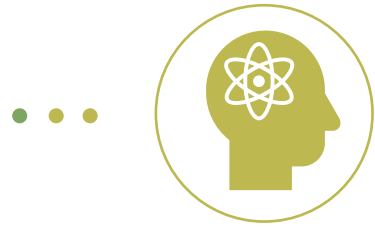
Software
Performance Measurement
Performance Attribution
GIPS ® Composites
Risk Analytics



High end
Investment Management Firms



Sophisticated
Investment Management
Decision Process.



Sophisticated

Investment
Management
Decision Process



Derivative Instruments

- Futures
- Options
- Options on Futures
- Currency Forwards
- Repos
- Swaps
- Long / Short Strategies

Index Futures Contracts

e.g.

S&P 500 FUTURE (USD)

FTSE 100 Index Future (GBP)

What is an Index Futures Contract?

1 Obligation to purchase or sell a given basket of securities at a specified date and price (contract).

2 Exchange traded.

3 Require margin account

4 Daily P&L are marked-to-market (settle into margin account)

5 **Long** Position is *synthetically* equivalent to : **Borrowing Cash (short)** and **Buy Asset (Long)**

6 **Short** Position is *synthetically* equivalent to : **Lending Cash (Long)** and **Sell Asset (Short)**

7 Cost effective **surrogate** to buying or selling shares (great liquidity, minimal transaction fees)

E-mini S&P 500 Futures

CONTRACT SIZE	\$50 x S&P 500 Index
MINIMUM TICK	0.25 index points
DOLLAR VALUE OF ONE TICK	\$12.50 U.S. Dollars
PRODUCT SYMBOL	ES
TRADING HOURS	Sunday - Friday 5:00p.m. - 4:00p.m. CT with a trading halt from 3:15p.m. - 3:30p.m. CT; Daily Maintenance period Monday - Thursday 4:00p.m. - 5:00p.m.
CONTRACT MONTHS	Nearest five months in the quarterly cycle (Mar, Jun, Sep, Dec)
OPTIONS AVAILABLE	Quarterly, Monthly, Weekly (Monday, Wednesday, Friday)

Source :www.cmegroup.com/trading/why-futures/welcome-to-e-mini-s-and-p-500-futures.html

S&P 500 E-Mini Jun '21 (ESM21)

4,227.00 +1.50 (+0.04%) 13:17 CT [CME]

4,226.75 x 137 4,227.25 x 138

CONTRACT SPECIFICATIONS for Tue, Jun 8th, 2021

Notional Value			
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$$\text{Size} \quad \times \quad \text{Price 0} \quad = \quad \text{Notional Value}$$

$$50 \quad \quad \quad 4\,000 \quad \quad \quad 200\,000 \text{ USD}$$

$$\text{Price 1} \quad \quad \quad \text{Notional Value}$$

$$4\,280 \quad = \quad 214\,000 \text{ USD}$$

$$(P_1 - P_0) \times 50 = \text{Gain} \quad = \quad 14\,000 \text{ USD}$$

Buy Securities

vs

Engage Future Contract



Must exchange cash to get exposure.



Just initial margin



Has a real market value.



Just notional P&L



P&L Marked-to-market daily.



Offers equity exposure



Offers currency exposure



Except on P&L

Simple Example

50% US Equities - Stocks only

	Portf		Bench		Allocation	Selection	Total
	Wgt	ROR	Wgt	ROR			
Cash	50%	3.00%	20%	3.00%	-1.68%	0.00%	-1.68%
US Equities	50%	10.00%	80%	10.00%	-0.42%	0.00%	-0.42%
Total	100%	6.50%	100%	8.60%	-2.10%	0.00%	-2.10%

Outcome:

Underperformed by **-2.10%**

Because Under Weighted US Equities **50% vs 80%**

$$Allocation = (W_P^k - W_B^k) \times (R_B^k - R_B^T)$$

Brinson-Fachler

Manager's decision:

Intent: Increase Equity exposures to 90%

Action: Buy additional equities worth \$5.6M

How does attribution results look like?

Strategy

Increase US Equity Exposures to 90%

	Portf		Bench	
	Wgt	ROR	Wgt	ROR
Cash	10%	3.00%	20%	3%
US Equities	90%	10.00%	80%	10%
Total	100%	9.30%	100%	8.60%

By buying more equities

	Allocation Selection		Total
Cash	0.56%	0.00%	0.56%
US Equities	0.14%	0.00%	0.14%
Total	0.70%	0.00%	0.70%

Story

Good Asset Allocation Decision

No Selection Effect

The story makes sense.

Reflects the intent of the manager's investment decision

Manager's decision:

Inten: Increase Equity exposures to 90%

Action: Engage in a future contract. Notionally equivalent to \$5.6M

How does attribution results look like?

Should the Story be the same?

Strategy

Increase US Equity Exposures to 90% by engaging into Future Contract

The Attribution Story ?

1. Recognize P&L on Future

	Allocation Selection		Total
Cash	-1.68%	0.00%	-1.68%
US Equities	-0.42%	2.80%	2.38%
Total	-2.10%	2.80%	0.70%

Story # 1

Bad Asset Allocation Decision
US Equity Stock Picker is a star



+ 2. Adjust Notional Exposure

	Allocation Selection		Total
Cash	0.56%	1.20%	1.76%
US Equities	0.14%	-1.20%	-1.06%
Total	0.70%	0.00%	0.70%

Story # 2

Good Asset Allocation Decision
Cash Security Picker is a star
US Equity Stock Picker is really bad



+ 3. Account for Cost-of-Carry

	Allocation Selection		Total
Cash	0.56%	0.00%	0.56%
US Equities	0.14%	0.00%	0.14%
Total	0.70%	0.00%	0.70%

Story # 3

Good Asset Allocation Decision
No Selection Effect



To tell a meaningful story ...

- 1. Recognize P&L on Future**
- 2. Adjust Notional Exposures (Cash & Equities)**
- 3. Account for Cost-of-Carry (Risk Free Rate)**
- 4. Organize the data the way the portfolio is managed**

Group futures positions
according to

Purpose

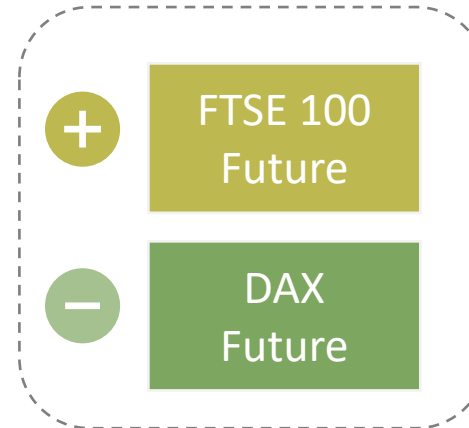
Intentions of manager

Increase exposure
to UK Equity

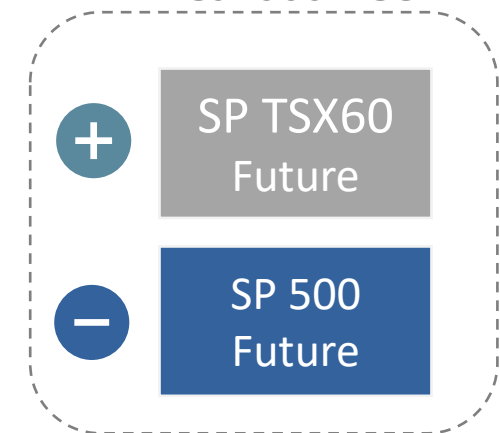
Alpha
Long/Short Strategies



+ U.K. - Germany



+ Canada - USA





The Purpose of Attribution

- Tell a **Story**
- Explains the excess return
- In a way that REFLECTS INVESTMENT DECISIONS MADE BY THE MANAGER(S)

The Art of Attribution

- Art of crafting the right attribution model
- Reflects investment decision process
- No matter how complex it may be

Artist: Performance Analyst

- Understand the investment process
- Configure attribution model accordingly
- Tells the **Story**

Review some Concepts

1

Concept of **Notional Value**

2

Differentiation between **Market** and **Currency** Exposures

3

Relationship between **index** price and its **futures price** (Arbitrage Free Theory)

4

Concept of **cost-of-carry**. Referred as the *basis*, *i.e.* difference between cash price and futures' price

5

Cash Offset. Multi-leg instrument (Long and Short legs)

6

Best practices

7

In the **context** of **Performance Measurement** and **Attribution**

E-mini S&P 500 Futures Specifications

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Source :www.cmegroup.com/trading/why-futures/welcome-to-e-mini-s-and-p-500-futures.html

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4,226.75 x 137 4,227.25 x 138

CONTRACT SPECIFICATIONS for Tue, Jun 8th, 2021

Size : 50

Price 0 : 4 000

Price 1 : 4 280

Nb. Contracts : 28

Notional Value : 5 600 000 USD

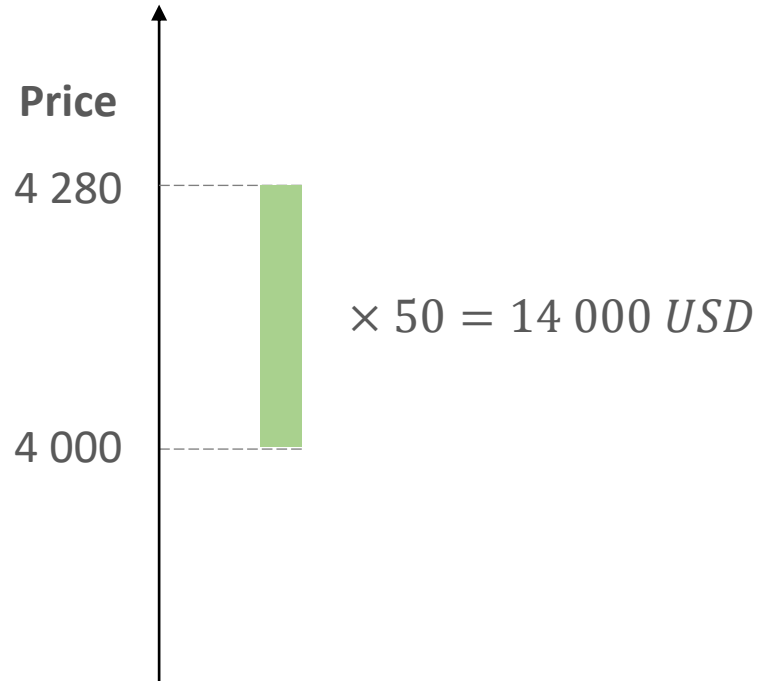
$P_0 \times Size \times Nb. Contracts$

Gain : 392 000 USD

$(P_1 - P_0) \times Size \times Nb. Contracts$

Mini S&P 500

Notional Value



Denominator (Notional Value) $4\,000 \times 50 \times 28 = 5\,600\,000\ USD$

Profit $(4\,280 - 4\,000) \times 50 \times 28 = 392\,000\ USD$

$$\frac{392\,000}{5\,600\,000} = 7\%$$

But you do not spend the money to buy the assets!

The money you keep can be invested at the risk free rate



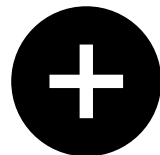
"There's no such thing as a free lunch."

Milton Friedman

July 31, 1912 – November 16, 2006



Benefit from the price appreciation of some assets



Without buying the assets



Cost

Arbitrage Free Theory

2.3 The price relationship between index and its futures price

The best-known model for pricing stock index futures is undoubtedly the cost of carry model, developed by Cornell and French (1983a). The derivation of this model is based on a simple no-arbitrage argument that two different assets, or combinations of assets, that yield the same return should sell for the same price. Otherwise, arbitrage profit is

Source:

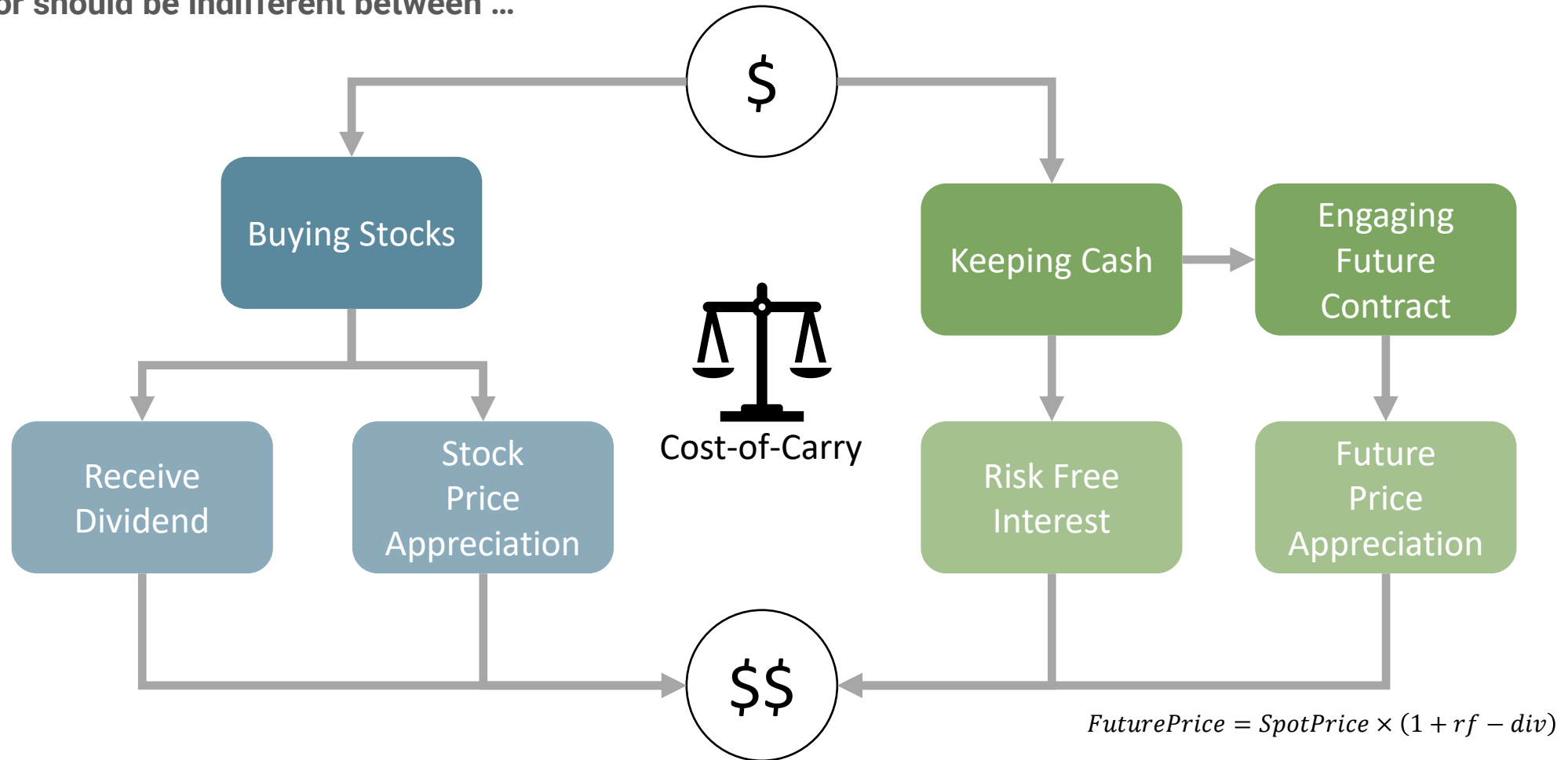
A re-examination of the relationship between FTSE100 index and futures prices
Juan Tao, 2008 <https://dspace.lboro.ac.uk/2134/8071>

Reference

Cornell, Bradford and French, Kenneth R., (1983), The pricing of stock index futures, Journal of Futures Markets, 3, issue 1, p. 1-14.

Arbitrage Free Theory

Investor should be indifferent between ...



Keep in mind that ...

Stocks
Return

≠

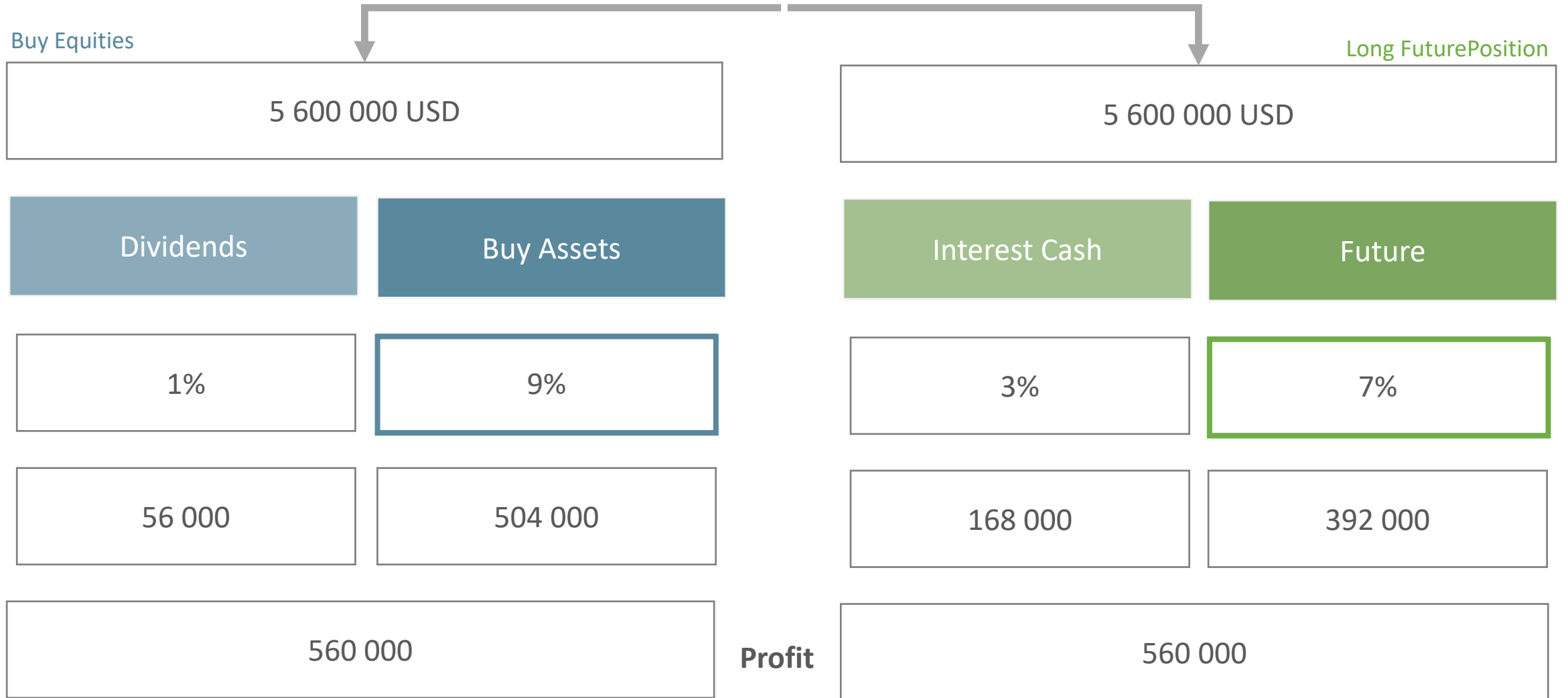
Future
Return

Generates Selection Effect

Unless you adjusted for the
Cost-of-Carry

Arbitrage Free Theory

Investor should be indifferent between ...



What if we only ...

1. Recognize P&L on Future

~~2. Adjust Notional Exposures (Cash & Equities)~~

~~3. Account for Cost-of-Carry (Risk Free Rate)~~

How attribution results looks like?

What story are you telling?

1. Recognize P&L on Future

2. ~~Adjust Notional Exposures (Cash & Equities)~~

3. ~~Account for Cost-of-Carry (Risk Free Rate)~~

	Weight	Mkt Val	Cap	Inc	Total Gain	ROR
Portfolio	100%	14,000,000	1,022,000	280,000	1,302,000	9.30%
Cash	50%	7,000,000	-	210,000	210,000	3.00%
Cash USD	48%	6,720,000	-	201,600	201,600	3.00%
Margin USD	2%	280,000	-	8,400	8,400	3.00%
US Equities	50%	7,000,000	1,022,000	70,000	1,092,000	15.60%
SP500 Stocks	50%	7,000,000	630,000	70,000	700,000	10.00%
Future	0%		392,000		392,000	#DIV/0!

Return OK

Return **not notionally meaningful**

Not Security Level Return

Allocation **not notionally meaningful**

Recognize Future P&L

1. Recognize P&L on Future

2. ~~Adjust Notional Exposures (Cash & Equities)~~

3. ~~Account for Cost-of-Carry (Risk Free Rate)~~

	Portf		Bench		Allocation Selection		Total
	Wgt	ROR	Wgt	ROR			
Cash	50%	3.00%	20%	3%	-1.68%	0.00%	-1.68%
US Equities	50%	15.60%	80%	10%	-0.42%	2.80%	2.38%
Total	100%	9.30%	100%	8.60%	-2.10%	2.80%	0.70%

Outcome:
 Outperformed by **0.70%**
 Allocation **-2.10%**
 Selection **2.80%**

- Added Value OK
- Selection not meaningful
- Allocation not meaningful

Is the Story Meaningful?
 Does it reflect the decision of the manager?



How do we fix that?

2. Recognize Notional Value of Future Contract



Let's do that ...

1. Recognize P&L on Future
2. Adjust Notional Exposures (Cash & Equities)
3. ~~Account for Cost-of-Carry (Risk Free Rate)~~

	Weight	Mkt Val	Cap	Inc	Total Gain	ROR
Portfolio	100%	14,000,000	1,022,000	280,000	1,302,000	9.30%
Cash	10%	1,400,000	-	210,000	210,000	15.00%
Cash USD	48%	6,720,000	-	201,600	201,600	3.00%
Margin USD	2%	280,000	-	8,400	8,400	3.00%
Contra	-40%	(5,600,000)			-	-
US Equities	90%	12,600,000	1,022,000	70,000	1,092,000	8.67%
Stocks	50%	7,000,000	630,000	70,000	700,000	10.00%
Future	40%	5,600,000	392,000		392,000	7.00%

Return OK

Cash Return **not** notionally meaningful

Return "OK" but not adjusted for cost-of-carry.

Allocation **notionally** meaningful

How attribution results looks like?
What story are you telling?

1. Recognize P&L on Future
2. Adjust Notional Exposures (Cash & Equities)
3. ~~Account for Cost-of-Carry (Risk Free Rate)~~

	Portf		Bench		Allocation Selection		Total
	Wgt	ROR	Wgt	ROR			
Cash	10%	15.00%	20%	3%	0.56%	1.20%	1.76%
US Equities	90%	8.67%	80%	10%	0.14%	-1.20%	-1.06%
Total	100%	9.30%	100%	8.60%	0.70%	0.00%	0.70%

Outcome:
 Outperformed by **0.70%**
 Allocation **0.70%**
 Selection **0.00%**

Added Value OK

Selection with Cash & Equity



Is the Story Meaningful?
 The story conveys **misleading Selection** Effects?

How do we fix that?

2. Recognize Notional Value of Future Contract

3. Account for Cost-of-Carry



Let's do that ...

1. Recognize P&L on Future
2. Adjust Notional Exposures (Cash & Equities)
3. Account for Cost-of-Carry (Risk Free Rate)

	Weight	Mkt Val	Cap	Inc	Total Gain	ROR
Portfolio	100%	14,000,000	1,022,000	280,000	1,302,000	9.30%
Cash	10%	1,400,000	-	42,000	42,000	3.00%
Cash USD	48%	6,720,000	-	201,600	201,600	3.00%
Margin USD	2%	280,000	-	8,400	8,400	3.00%
Contra	-40%	(5,600,000)		(168,000)	(168,000)	3.00%
US Equities	90%	12,600,000	1,022,000	238,000	1,260,000	10.00%
Stocks	50%	7,000,000	630,000	70,000	700,000	10.00%
Future	40%	5,600,000	392,000	168,000	560,000	10.00%

Return OK

Cash Return
notionally
meaningful

Return adjusted
for cost-of-carry.

Transfer notional
income (risk free)

How attribution results looks like?
What story are you telling?

1. Recognize P&L on Future
2. Adjust Notional Exposures (Cash & Equities)
3. Account for Cost-of-Carry (Risk Free Rate)

	Portf		Bench		Allocation Selection		Total
	Wgt	ROR	Wgt	ROR			
Cash	10%	3.00%	20%	3%	0.56%	0.00%	0.56%
US Equities	90%	10.00%	80%	10%	0.14%	0.00%	0.14%
Total	100%	9.30%	100%	8.60%	0.70%	0.00%	0.70%

Outcome:
 Outperformed by **0.70%**
 Allocation **0.70%**
 Selection **0.00%**

Added Value OK

Selection with Cash & Equity OK

The Story is Meaningful?
 REFLECTS THE INVESTMENT DECISION PROCESS



Recap

	Portf		Bench		Allocation Selection		Total
	Wgt	ROR	Wgt	ROR			
Cash	50%	3.00%	20%	3%	-1.68%	0.00%	-1.68%
US Equities	50%	15.60%	80%	10%	-0.42%	2.80%	2.38%
Total	100%	9.30%	100%	8.60%	-2.10%	2.80%	0.70%

	Portf		Bench		Allocation Selection		Total
	Wgt	ROR	Wgt	ROR			
Cash	10%	15.00%	20%	3%	0.56%	1.20%	1.76%
US Equities	90%	8.67%	80%	10%	0.14%	-1.20%	-1.06%
Total	100%	9.30%	100%	8.60%	0.70%	0.00%	0.70%

	Portf		Bench		Allocation Selection		Total
	Wgt	ROR	Wgt	ROR			
Cash	10%	3.00%	20%	3%	0.56%	0.00%	0.56%
US Equities	90%	10.00%	80%	10%	0.14%	0.00%	0.14%
Total	100%	9.30%	100%	8.60%	0.70%	0.00%	0.70%

Story #1

1. Recognize P&L on Future

- US Stock Picker is a star
- Asset Allocator made bad decision

Story #2

2. Adjust Notional Exposures

- Cash Stock Picker is a star
- US Stock Picker made bad decision
- Asset Allocator made good decision

Story #3

3. Account for Cost-of-Carry

- No Security Selection
- Asset Allocator made good decision

What about Futures in Foreign Markets?

What is the Currency Exposure of a Future Contract?



FTSE 100 Index Future – London Stock Exchange

Market Specifications

Trading Screen Product Name

FTSE 100 - Stnd Index Future

Trading Screen Hub Name

ICEU

Commodity Code

Z

Unit of Trading

Contract Valued at £10 per index point (e.g. value £65,000 at 6,500.0)

Delivery Months

Four quarterly months from in the March, June, September, December quarterly cycle

Settlement Date

First business day after the Last Trading Day

Quotation

Index points (eg 6500.0)

Minimum price movement (tick size and value)

0.5 (£5.00)

FTSE Futures

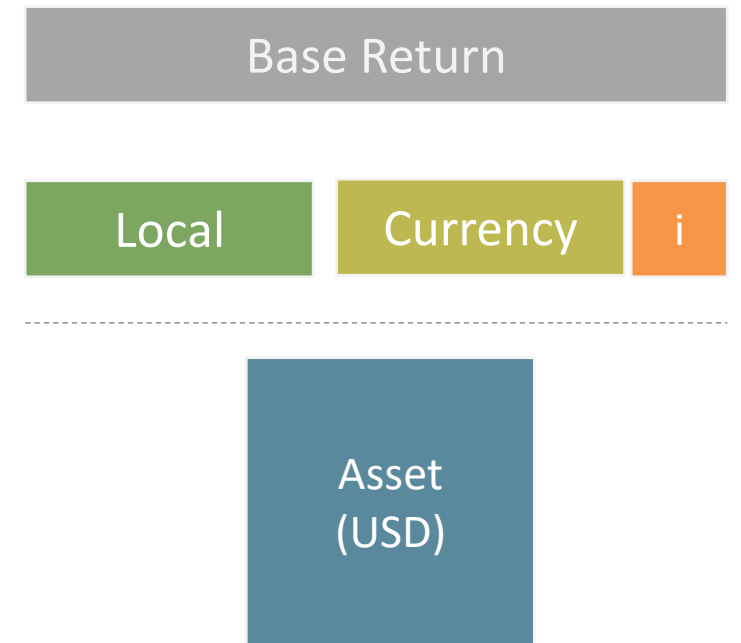
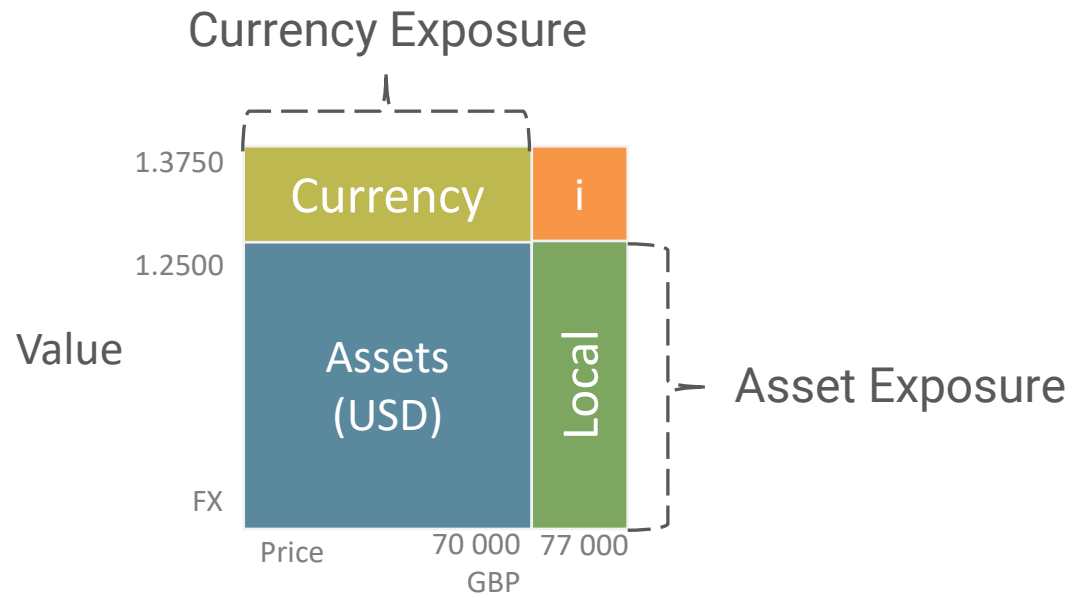
Symbol	Last	Chg
FTSE 100 FUTURES	7,106.80	+25.30

Open Last Trade : 13:39

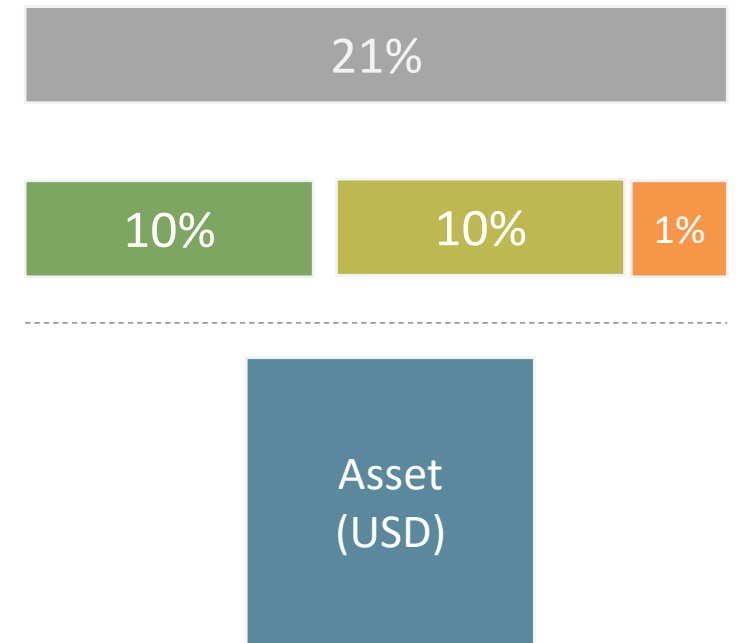
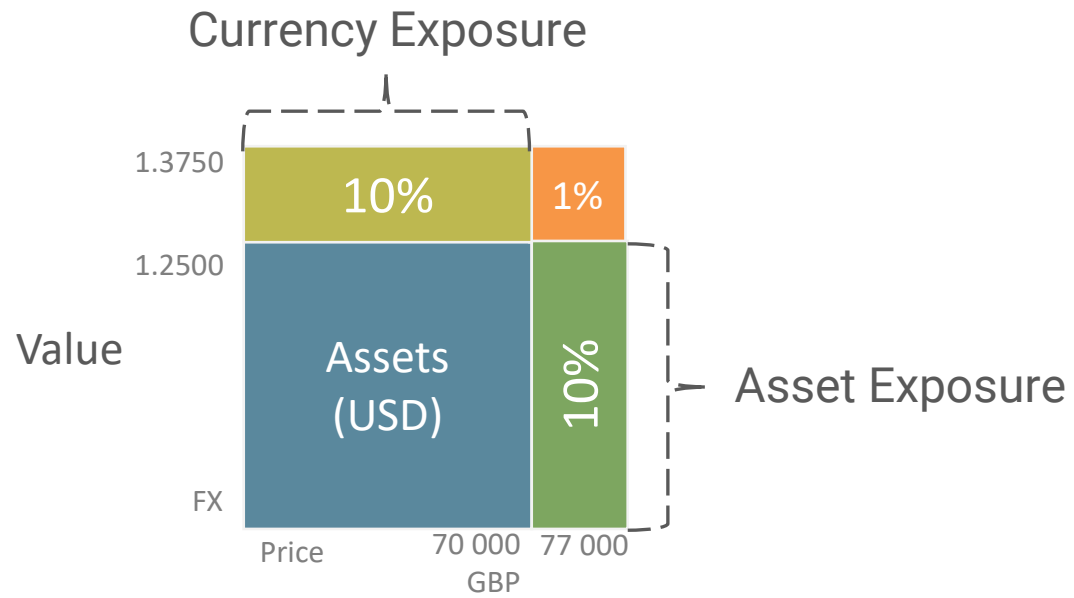
UK Time : Tue Jun 08 2021 13:39

$$\begin{array}{rcccl} \text{Multiplier} & & \text{Price} & & \text{Notional Value} \\ & \times & & = & \\ & 10 & 7\ 000 & & 70\ 000\ \text{GBP} \end{array}$$

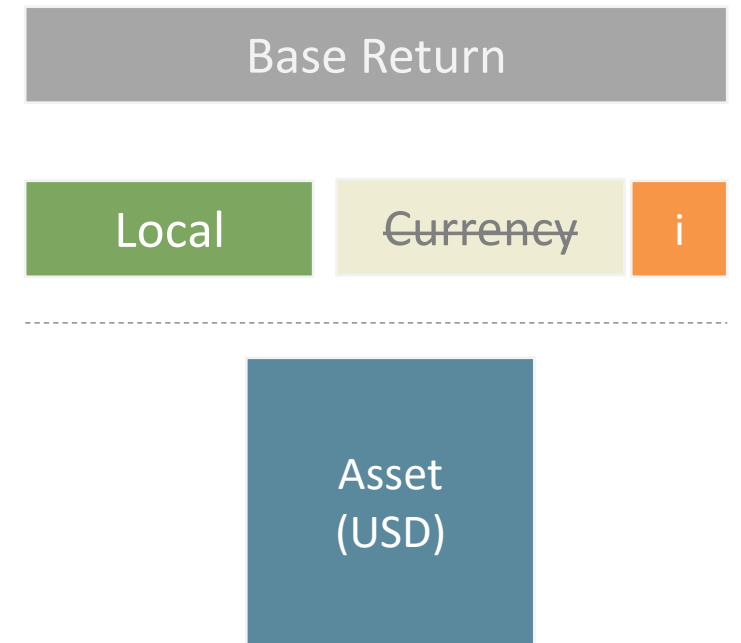
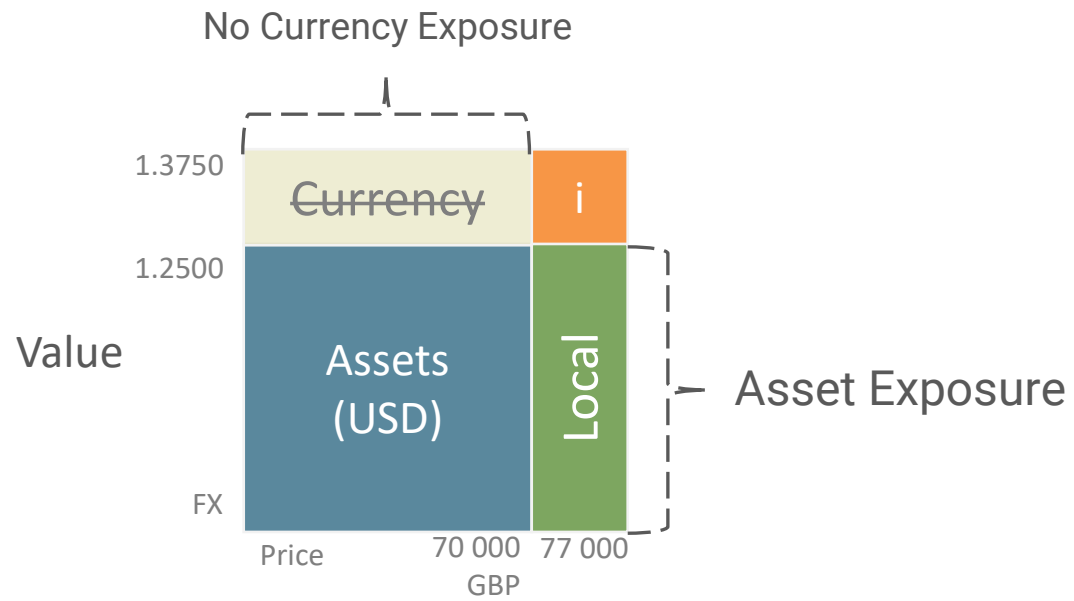
Exposures – Stocks



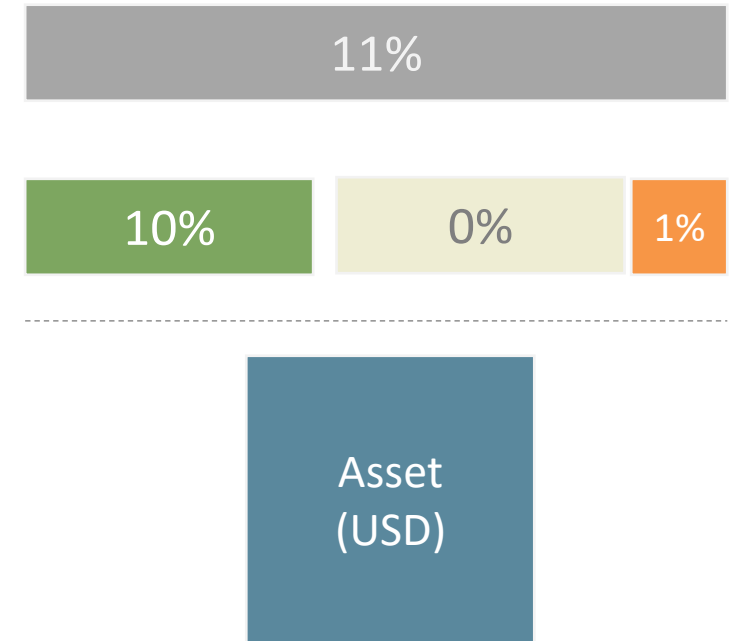
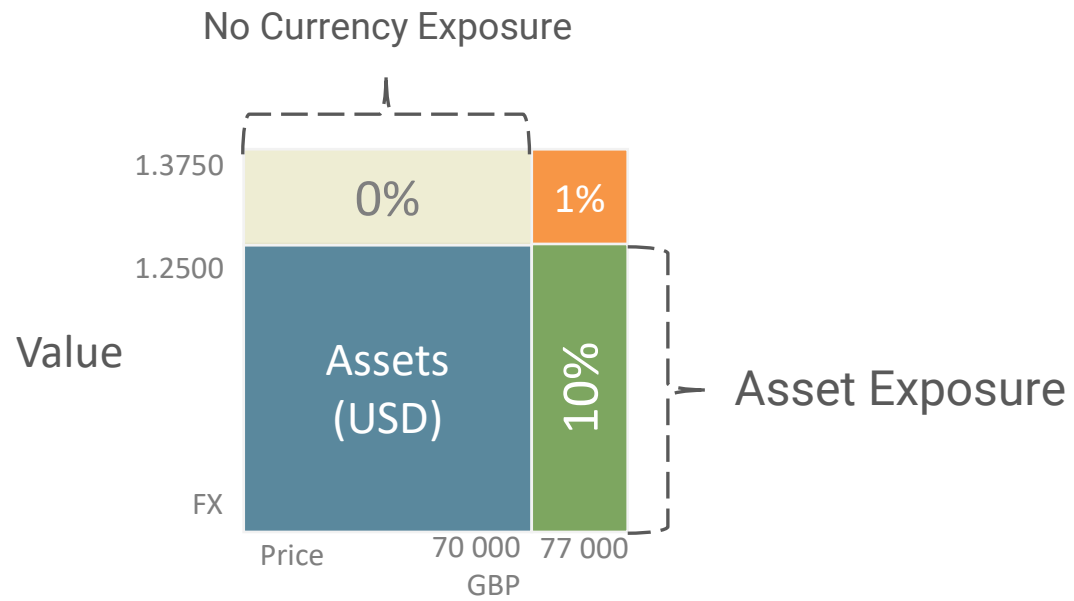
Returns – Stocks



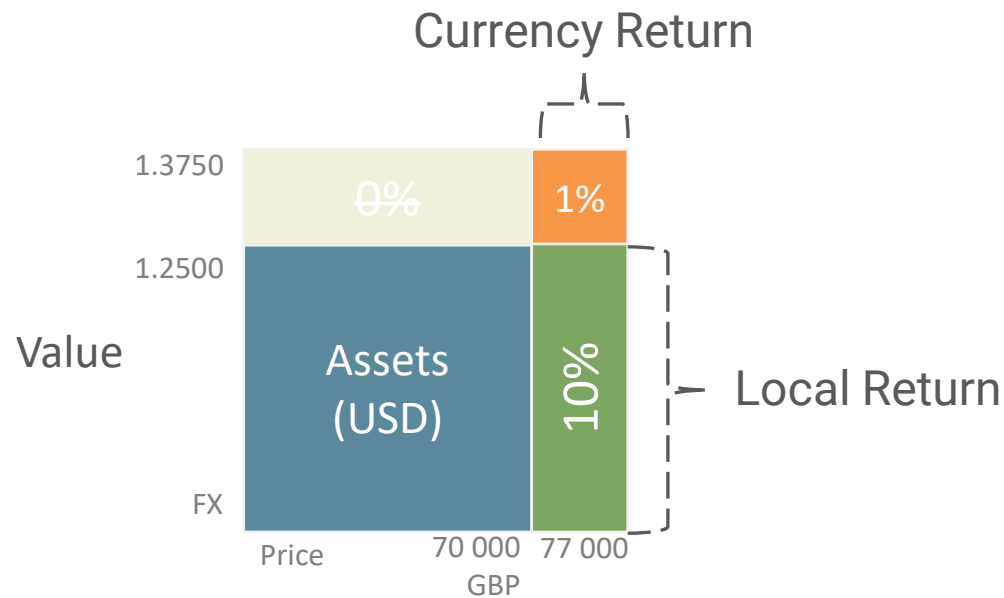
Exposures – Futures



Returns – Futures



Base, Local and Currency Returns – Futures



11%

10%

1%

Local Return

$$= \frac{7\,000}{70\,000} = 10\% \text{ GBP}$$

Currency Return

$$\frac{7\,000 \times (1.375 - 1.250)}{70\,000 \times 1.25}$$

$$= \frac{875}{87\,500} = 1\% \text{ USD}$$

www.RobustTechnologies.com

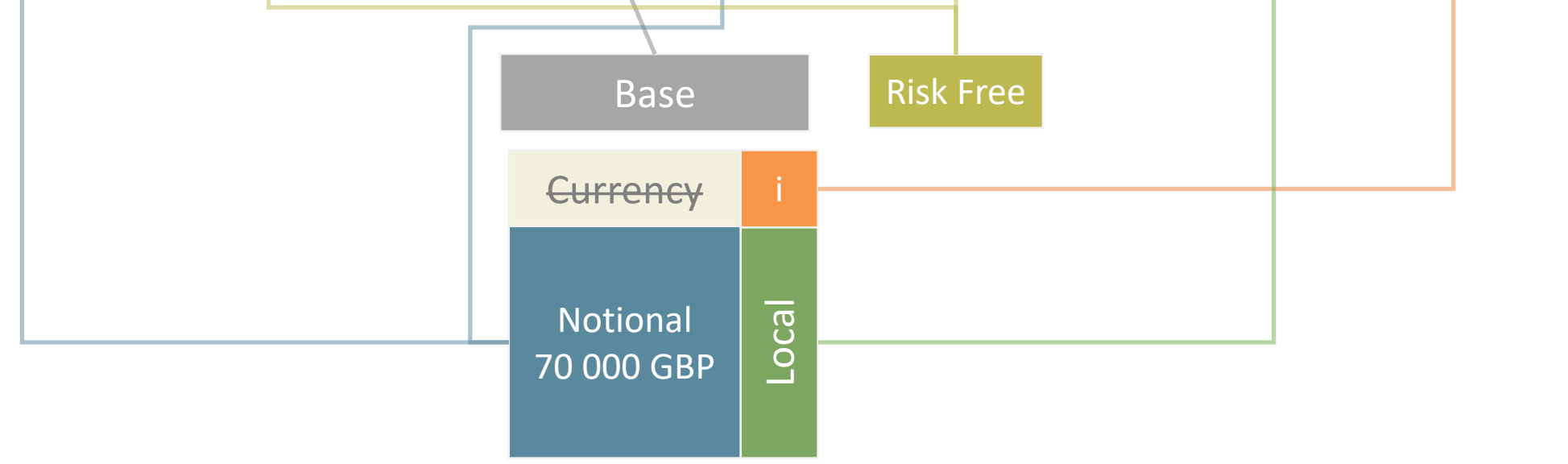
Base Return

$$\frac{(7\,000 \times 1.250) + 875}{70\,000 \times 1.25}$$

$$\frac{9\,625}{87\,500} = 11\% \text{ USD}$$

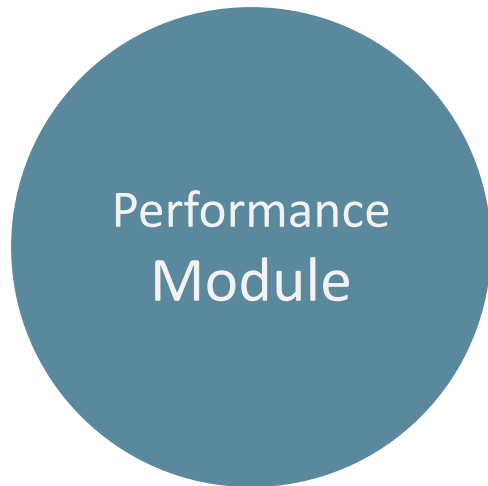
Powered by Robust Technologies

Issuer	Price Begin	Price End	Base (USD)								Local								Currency		
			Begin Market Value	End Market Value	Cash Flows	Cost of Carry	\$ Earned	Weight	TW Contribution	Time Weighted Return	Begin Market Value	End Market Value	Cash Flows	Cost of Carry	\$ Earned	\$ Earned (Base)	TW Contribution	Time Weighted Return	\$ Earned (Base)	TW Contrib	TW Return
Total Structure	-	-	212,500	254,238	-	-	41,738	100.00%	19.64%	19.64%	170,000	184,900	-	-	14,900	18,625	8.76%	8.76%	23,113	10.88%	10.88%
Cash	-	-	125,000	149,325	7,700	-	16,625	58.82%	7.82%	13.30%	100,000	108,600	5,600	-	3,000	3,750	1.76%	3.00%	12,875	6.06%	10.30%
CASH - GBP	1.00	1.00	62,500	71,775	963	-	8,313	29.41%	3.91%	13.30%	50,000	52,200	700	-	1,500	1,875	0.88%	3.00%	6,438	3.03%	10.30%
MARGINUS	1.00	1.00	62,500	77,550	6,738	-	8,313	29.41%	3.91%	13.30%	50,000	56,400	4,900	-	1,500	1,875	0.88%	3.00%	6,438	3.03%	10.30%
Contra Futures	-	-	-87,500	-102,988	-6,738	-2,625	-	-41.18%	-1.24%	3.00%	-70,000	-74,900	-4,900	-2,100	-	-	-1.24%	3.00%	-	-	-
FTSE 100 FUTURE	-	-	-87,500	-102,988	-6,738	-2,625	-	-41.18%	-1.24%	3.00%	-70,000	-74,900	-4,900	-2,100	-	-	-1.24%	3.00%	-	-	-
Equities	-	-	175,000	207,900	-963	2,625	25,113	82.35%	13.05%	15.85%	140,000	151,200	-700	2,100	11,900	14,875	8.24%	10.00%	10,238	4.82%	5.85%
FTSE 100 FUTURE	7,000.00	7,490.00	87,500	102,988	-	2,625	6,737.50	41.18%	4.41%	10.70%	70,000	74,900	-	2,100	4,900	6,125	4.12%	10.00%	612.50	0.29%	0.70%
Stocks	100.00	109.00	87,500	104,913	-963	-	18,375.00	41.18%	8.65%	21.00%	70,000	76,300	-700	-	7,000	8,750	4.12%	10.00%	9,625.00	4.53%	11.00%



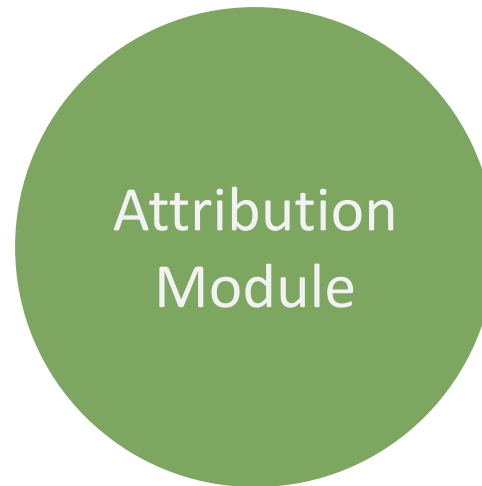
Adjusting for

Notional Exposure
Cost-of-Carry
Currency Exposure



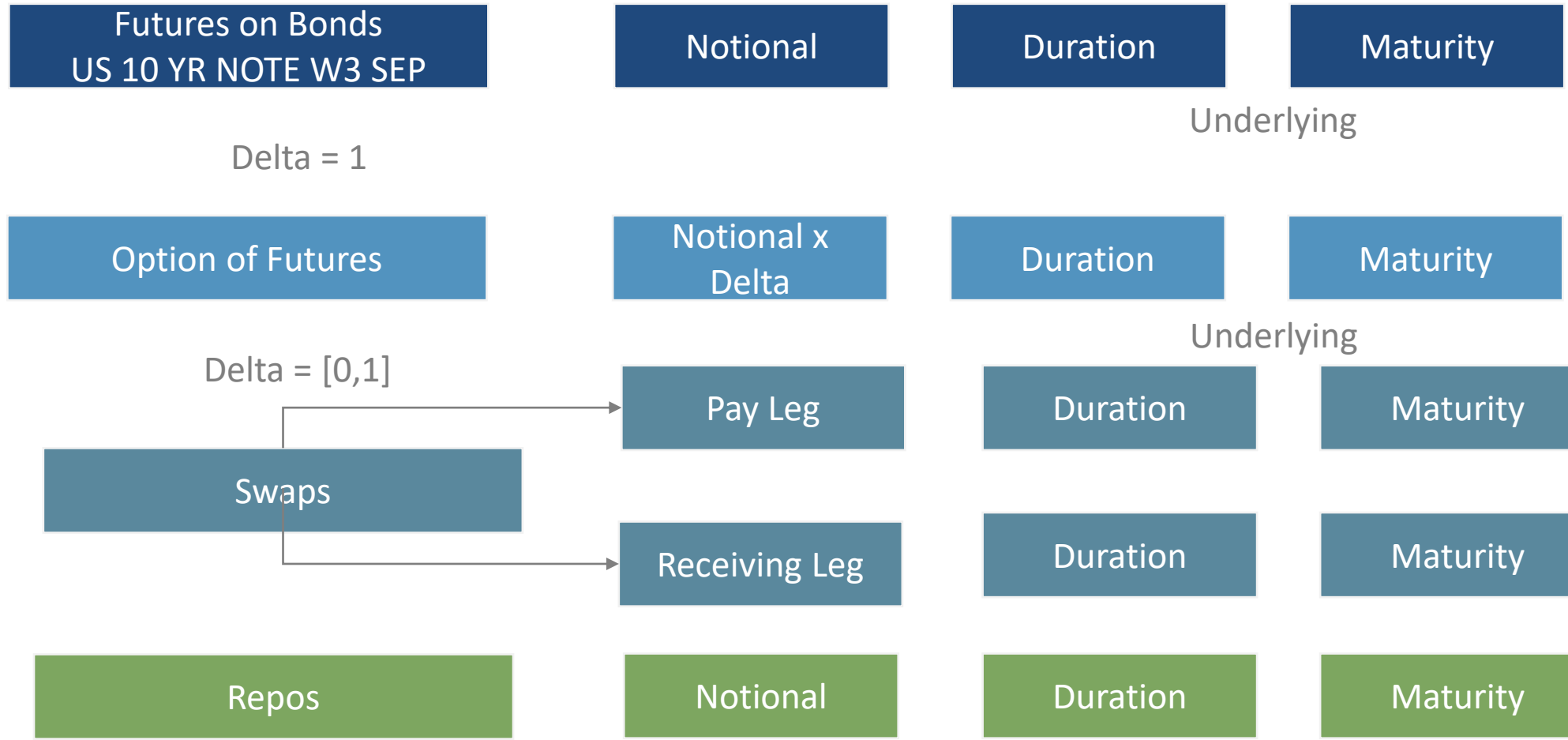
Requires

No change



- ✓ Equity Attribution
- ✓ Fixed Income Attribution
- ✓ Multi Asset Attribution
- ✓ Currency Attribution
- ✓ Security Level Attribution

Other derivatives...



In summary

- Must reflect notional exposure (using Current Price)
- Offset exposure to Cash (Cash Offset)
 - Long position : Borrow cash (short) – Buy assets (long)
 - Short position : Lend cash (long) – Sell assets (short)
- Group Future Cash Offset and Variation Margin together (in Cash Equivalents)
- Marked-to-Market P&L still considered as asset exposure (not cash) until the future position is liquidated.

In summary

- Must properly recognize the type of exposures.
 - Asset vs Currency
 - Future on FTSE 100 does not offer currency exposure (GBP)
 - Only asset exposure
 - The only impact on currency return is FX Rates variation on Future P&L settled in GBP

In summary

- Must adjust for Cost-of-Carry (risk free rate)
 - Represent opportunity cost of purchasing the assets rather than engaging in a future contract.
 - To reflect the cost of carry. Referred as the basis, i.e. difference between cash price and futures' price (generally risk free rate minus expected dividends)
 - Makes return comparable to underlying assets in the benchmark
 - Other wise Selection effect is generated

References



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John C. Stannard, Russell Data Services

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Measuring Investment Returns of Portfolios Containing Derivatives: Part II -
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John C. Stannard, Russell Data Services

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The **reporting** and
performance measurement
of financial **futures** and **options**
in **investment portfolios**

prepared in conjunction with

WILLIAM M.
MERCER

LIFFE Recommendations
January 1992

LIFFE

The London International Financial
Futures and Options Exchange

Thank you !

Questions or Comments ?

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